

## Spin-hall-active platinum thin films grown via atomic layer deposition

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We study the magnetoresistance of yttrium iron garnet/Pt heterostructures in which the Pt layer was grown via atomic layer deposition (ALD). Magnetotransport experiments in three orthogonal rotation planes reveal the hallmark features of spin Hall magnetoresistance. To estimate the spin transport parameters, we compare the magnitude of the magnetoresistance in samples with different Pt thicknesses. We check the spin Hall angle and the spin diffusion length of the ALD Pt layers against the values reported for high-quality sputter-deposited Pt films. The spin diffusion length of 1.5 nm agrees well with that of platinum thin films reported in the literature, whereas the spin Hall magnetoresistance  $\Delta\rho/\rho = 2.2 \times 10^{-5}$  is approximately a factor of 20 smaller compared to that of our sputter-deposited films. Our results demonstrate that ALD allows fabricating spin-Hall-active Pt films of suitable quality for use in spin transport structures. This work provides the basis to establish conformal ALD coatings for arbitrary surface geometries with spin-Hall-active metals and could lead to 3D spintronic devices in the future. *Published by AIP Publishing.*

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Atomic layer deposition (ALD) is a powerful process that allows 3D conformal coatings.<sup>1</sup> ALD has been extensively used for the deposition and conformal coating of thin oxide insulator films onto nanopatterned templates or flat substrates. Over the last few years ALD processes have also been developed for a number of metals.<sup>1,2</sup>

In particular, the ALD of Pt has been investigated by several groups. Different precursor chemistries based on trimethyl(methylcyclopentadienyl)platinum, Pt(CpMe)Me<sub>3</sub>,<sup>3,4</sup> or platinum acetylacetonate, Pt(acac)<sub>2</sub>,<sup>5</sup> have been reported, with the former generally resulting in films with higher conductivity.

Pt with its strong spin-orbit coupling is one of the key materials for modern spintronics, allowing the efficient conversion of charge currents to spin currents and vice versa, i.e., leading to a large spin Hall effect.<sup>6,7</sup> Thus, the ALD of Pt could open the door for 3D metallic nanostructures with spintronic functionality, for instance, structures dependent on high aspect ratios, such as racetrack memory.<sup>8,9</sup>

Additionally, interesting phenomena related to spin transport in non-planar geometries (e.g., coated nanowires) were recently proposed.<sup>10</sup> For example, the propagation length of spin/magnon currents in such curved geometries should crucially depend on the spin current polarization vector.<sup>10–12</sup>

To determine by electrical transport whether spin generation and detection are also feasible in such structures, spin Hall magnetoresistance (SMR) can be used. SMR is a potent tool for determining the spin transport parameters in ferromagnetic insulator (FMI)/non-ferromagnetic metal (NM) heterostructures.<sup>7,13,14</sup> Most importantly, the magnitude of the SMR effect as a function of the NM thickness allows inferring the spin Hall angle  $\Theta_{SH}$  and the spin diffusion length  $\lambda_{NM}$  of the normal metal and the FMI/NM interface quality quantified by the spin mixing conductance  $G_r$ .<sup>13</sup>

Here, we show that Pt films grown via ALD are indeed spin Hall active. Specifically, we observe an SMR with a magnitude of  $2.2 \times 10^{-5}$  in heterostructures consisting of an yttrium iron garnet (Y<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>, YIG) thin film covered by a Pt layer grown by ALD. This is clear evidence for spin-Hall-driven spin current transport across the YIG/Pt interface. Thus, our study establishes the ALD deposition of Pt, a prototypical material that is widely used as a detector/injector for spin currents. This provides an important contribution towards the realization of spin transport experiments in non-planar/non-trivial geometries and might lead to spintronic applications in 3D geometries in the future.

We started from commercially available, 1 μm thick YIG films grown via liquid phase epitaxy on Gd<sub>3</sub>Ga<sub>5</sub>O<sub>12</sub> substrates. Then, we used the established cleaning and pre-preparation procedure to prepare our *ex situ* YIG/Pt samples.<sup>15,16</sup>

The YIG films were cleaned using piranha etching solution (3H<sub>2</sub>SO<sub>4</sub>:1H<sub>2</sub>O<sub>2</sub>) for 1 min to remove organic residue

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from the surface.<sup>16</sup> Subsequently, the samples were submerged in distilled or de-ionized water and loaded into the ALD chamber while still covered with water. The two different sets of equipment and parameters that were used for growing the Pt films are denoted as series A and series B.

The growth of series A was performed in a commercially available GemStar XT-R thermal bench-top ALD system from Arradiance. Me(CpPt)Me<sub>3</sub> was used as the Pt precursor with pure oxygen (O<sub>2</sub>) as the oxidizer. The chamber temperature was set to 250 °C, and the organic precursor was pre-heated to 68 °C in order to increase the evaporation rate. The pulse and exposure times of the Me(CpPt)Me<sub>3</sub> were set to 50 ms and 20 s, respectively, followed by a 60 s pumping time for the removal of any residual precursor and the reactants. For pulsing the Pt precursor, the so-called boost mode was used, in which Ar was inserted into the Me(CpPt)Me<sub>3</sub> precursor bottle to increase the amount of precursor inserted into the chamber. For the second half-cycle, O<sub>2</sub> was pulsed for 20 ms with subsequent exposure and pumping times of 4 s and 60 s, respectively. For the samples grown within series A, 100 and 280 cycles were performed, resulting in thicknesses of  $t_{\text{Pt}} = (4.4 \pm 1)$  nm and  $t_{\text{Pt}} = (19.0 \pm 1)$  nm, respectively.

The platinum films for series B were grown in a Gemstar-6 ALD reactor, which is also commercially available from Arradiance. The same organic precursor was used, but the oxidizer was replaced with ozone (O<sub>3</sub>) due to its higher reactivity. The ozone was provided by a BMT 803N ozone generator. The organic precursor was heated to 50 °C, while the reactor chamber was set to 220 °C. The pulse and exposure times of the Pt precursor were set to 500 ms and 30 s, respectively. The pulse and exposure steps were performed two times to ensure a saturation of the sample surface with the organic precursor. Afterwards, the precursor residue and the reactants were purged from the chamber in a 90 s pump interval. Subsequently, O<sub>3</sub> was pulsed for 500 ms, followed by an exposure time of 30 s and a pump time of 90 s. With these parameters, for example, 240 cycles result in a Pt thickness of  $t_{\text{Pt}} = (14.3 \pm 0.5)$  nm. A summary of the growth parameters of both series A and B is presented in Table I.

Additionally, a reference sample was prepared with a 7 nm sputtered Pt film, where the YIG film was additionally annealed in the ultra-high-vacuum of the deposition chamber at 200 °C after the piranha etch to further improve the interfacial quality and to mimic the temperature of the ALD process.

To investigate the surface topology, atomic force microscopy (AFM) was performed to extract the rms roughness of

TABLE I. The growth parameters used in series A and B are summarized in this table. The process flow is defined by pulse times ( $t_p$ ), exposure times ( $t_{\text{exp}}$ ), and pump times ( $t_{\text{pump}}$ ).

	Series A	Series B
Chamber temperature $T_{\text{ch}}$ [°C]	250	220
Precursor temperature $T_{\text{Pt}}$ [°C]	68	50
Pt: $t_p/t_{\text{exp}}/t_{\text{pump}}$ [s]	0.05 <sup>a</sup> /20/60	0.5/30 <sup>b</sup> /90
O <sub>2</sub>  O <sub>3</sub> : $t_p/t_{\text{exp}}/t_{\text{pump}}$ [s]	0.02/4/60	0.5/30/90

<sup>a</sup>The precursor flow was increased using N<sub>2</sub> for the pulse time.

<sup>b</sup>The steps were performed twice before continuing with the process.

our films. An AFM measurement of a sample with  $t_{\text{Pt}} = 8.8$  nm yields a roughness of 0.72 nm that is consistent with that of comparable films shown in the literature.<sup>7</sup> Furthermore, the exact thickness of the films was determined by X-ray reflectometry (XRR) measurements and subsequent fitting of the obtained curves. An exemplary set of data and the respective fit are shown in Fig. 1(b).

Finally, we carried out X-ray diffraction measurements to infer the crystalline structure as well as the grain size. We find the sputtered as well as ALD grown films to be oriented preferentially along the (111) direction, with a full width at half maximum of the corresponding diffraction peaks of 0.8 deg and 0.9 deg for a sputtered film with  $t_{\text{Pt}} = 13.2$  nm and a film from series B with  $t_{\text{Pt}} = 14.1$  nm, respectively.

After the structural characterization, Hall bars were patterned into the Pt layers [cf. Fig. 1(a)] using optical lithography and subsequent dry etching with Ar ions. The Hall bars have a length of  $l = 400 \mu\text{m}$  and a width of  $w = 80 \mu\text{m}$ . To establish electrical contact to our setup, the samples were glued to a chip carrier and contacted via wedge bonding with aluminum wire. To quantify the magnetoresistive response, the samples were mounted in a magnet setup with a cylindrical Halbach array.<sup>17</sup> It features a constant magnetic flux density of  $\mu_0 H = 1$  T perpendicular to the array's cylindrical axis. To obtain the magnetoresistance, we drive a current of  $I = 80 \mu\text{A} - 500 \mu\text{A}$  along the Hall bar with a Keithley 2450 sourcemeter while simultaneously recording the voltage drop with a Keithley 2182 nanovoltmeter. To further improve the measurement sensitivity and to remove spurious contributions, we employ a current reversal technique.<sup>18</sup>

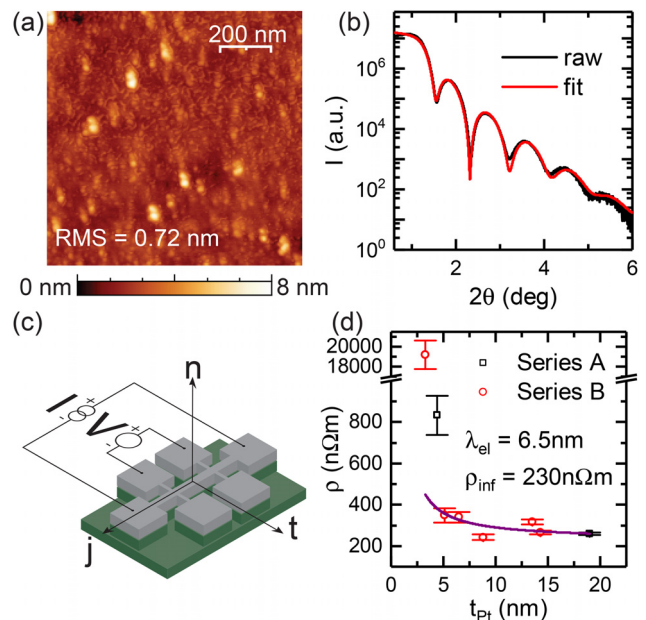


FIG. 1. Panel (a) depicts an exemplary AFM measurement of a YIG/Pt sample with  $t_{\text{Pt}} = 8.8$  nm, yielding an rms roughness of  $h = 0.72$  nm. An XRR measurement on the same sample and the respective fit are shown in panel (b). Panel (c) displays the sample structure after deposition and lithography. The contacts for the resistivity measurement and the coordinate system with respect to the Hall bar are also depicted here. The obtained resistivities for the two sample series are plotted in panel (d) as a function of the platinum thickness. A fit of Eq. (1) to the data yields an electron mean free path of  $\lambda_{\text{el}} = 6.5$  nm and a bulk platinum resistivity of  $\rho_{\text{inf}} = 230$  nΩm.

The resistivity of the samples as a function of the platinum thickness is shown in Fig. 1(d). As expected for platinum and all other metals, a sharp increase in the resistivity toward low thicknesses is observed, which is consistent with previous reports.<sup>19,20</sup> We use Eq. (1) to fit the data and extract the mean free path in our platinum layers assuming that we are in the diffusive limit.<sup>21</sup> The fit yields a bulk resistivity of  $\rho_{\text{inf}} = 230 \text{ n}\Omega\text{m}$  and an electron mean free path of  $\lambda_{\text{el}} = 6.5 \text{ nm}$  when using the roughness of  $h = 0.72 \text{ nm}$  as determined by AFM. For the two thinnest samples, the resistivity is much higher than expected, which we tentatively attribute to the nucleation delay of the Pt growth during the first 50–100 cycles as reported in the literature<sup>4</sup>

$$\rho(t_{\text{Pt}}) = \rho_{\text{inf}} \left( 1 + \frac{3\lambda_{\text{el}}}{8(t_{\text{Pt}} - h)} \right). \quad (1)$$

The extracted mean free electron path and the bulk resistivity agree well with values reported for evaporated platinum thin films.<sup>20</sup>

To determine the angular dependence of the magnetoresistance, the Halbach array and thus the magnetic field are rotated around the cylindrical axis. Using three different sample inserts, we define the (mutually orthogonal) rotation planes of the magnetic field. For in-plane rotations (ip), the magnetic field is rotated in the film plane around the surface normal  $\mathbf{n}$ . For the other two rotation planes, with a finite component of the magnetic field out of the film plane (oop), the magnetic field is either rotated around the direction of the current flow  $\mathbf{j}$  (oopj) or the transverse direction  $\mathbf{t}$  (oopt). The three rotation planes are shown as insets in Figs. 2(a)–2(c).

The obtained magnetoresistance for a YIG/Pt (ALD) film with  $t_{\text{Pt}} = 4.4 \text{ nm}$  is shown in Fig. 2. The resistivity of Pt is strongly temperature dependent; therefore, a linear drift was subtracted from the data to compensate for the slow drifts of the sample temperature. Since the SMR only depends on the projection of the magnetization onto the  $\mathbf{t}$  direction,<sup>7,13</sup> i.e.,  $\rho \propto m_t^2$ , we expect to observe a  $\sin^2(\alpha, \beta)$  modulation for the ip and oopj configurations and no modulation for the oopt rotation. This is fully corroborated by our experimental observations. In other words, Fig. 2 shows the characteristic fingerprint of SMR in our YIG/Pt heterostructures also for ALD-grown Pt.

The magnitude of the SMR for the sample shown in Fig. 2 is  $\Delta\rho/\rho = 2.2 \times 10^{-5}$ . Comparing these values to those of our reference sample with a sputtered Pt film

( $\Delta\rho/\rho = 3.6 \times 10^{-4}$ ), the SMR amplitude is reduced by a factor of 20 and is smaller by a factor of 40 when compared to that of the best YIG/Pt heterostructures with similar Pt thicknesses.<sup>7</sup> This result leads to two possible conclusions: either the interface of the heterostructure is not ideal or the quality of the Pt film is decreased by using ALD. However, the electrical characterization of our films contradicts the latter. Consequently, we assume that contributions such as organic contaminants at the interface or the cleaning procedure should be further optimized to take ALD-specific requirements into account.

Additionally, we recorded the transverse (Hall) voltage during the magnetic field rotations as well as magnetic field sweeps. From the linear slope, we extract an ordinary Hall coefficient of  $A_{\text{OHE}} = 46 \text{ p}\Omega\text{m T}^{-1}$  for a 5.1 nm thick sample. For a sample with 13.5 nm, we find  $A_{\text{OHE}} = 35 \text{ p}\Omega\text{m T}^{-1}$ . The trend and the magnitudes are in good agreement with previous reports of the thickness dependent ordinary Hall coefficient in sputtered platinum films on YIG.<sup>22</sup> Furthermore, a planar Hall effect is observed for the ip-rotations, having a  $\cos(\alpha) \sin(\alpha)$ -shaped angular dependence. The magnitude of this effect agrees with the longitudinal magnetoresistance (MR) data as expected for SMR.<sup>13</sup>

To further analyze the relevant transport parameters in our heterostructures, we investigate the thickness dependence of the SMR (c.f. Fig. 3). As expected for SMR, the magnitude of the MR decreases for increasing thickness<sup>13</sup>

$$\frac{\Delta\rho}{\rho} = \frac{2\Theta_{\text{SH}}^2 \lambda_{\text{Pt}}^2 \rho_{\text{Pt}} G_{\text{r}}}{t_{\text{Pt}}} \frac{\tanh^2\left(\frac{t_{\text{Pt}}}{2\lambda_{\text{Pt}}}\right)}{1 + 2\rho_{\text{Pt}} \lambda_{\text{Pt}} G_{\text{r}} \coth\left(\frac{t_{\text{Pt}}}{\lambda_{\text{Pt}}}\right)}. \quad (2)$$

Using two different sets of parameters adapted from the study by Althammer *et al.*<sup>7</sup> together with the bulk resistivity  $\rho = 230 \text{ n}\Omega\text{m}$  and Eq. (2), we can reproduce the trend of the thickness dependence (c.f. dark red and dark blue curves in Fig. 3).

However, to also obtain a good fit of the magnitude of our data, we have to reduce the spin mixing conductance by approximately a factor of 10. The two sets of parameters are summarized in Fig. 3. Additionally, from the two parameter sets, it is clear that the spin Hall angle and the spin mixing conductance are closely related and that their influence cannot be trivially separated. Nevertheless, all parameters agree well with the range of previously reported values.<sup>6</sup>

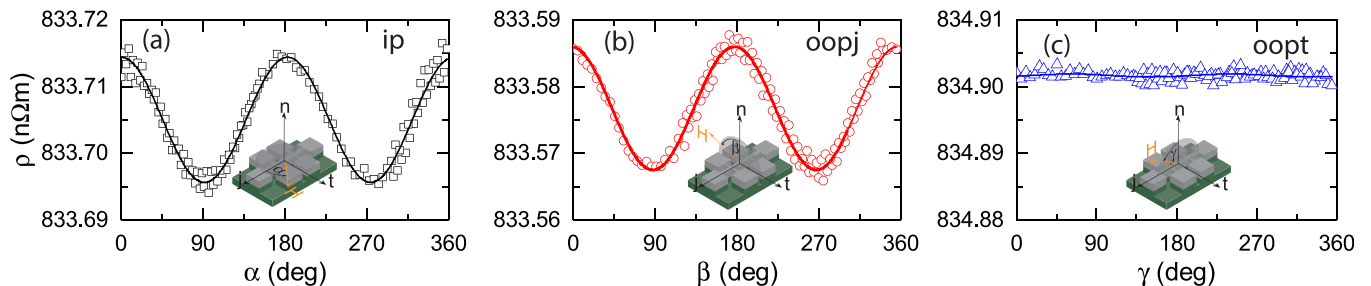


FIG. 2. The resistance of a YIG/Pt sample with  $t_{\text{Pt}} = 4.4 \text{ nm}$  obtained during rotations of the magnetic field in ip, oopj, and oopt configurations is shown in (a), (b), and (c), respectively. The definitions of the three orthogonal rotation planes ip, oopj, and oopt are shown as insets in the respective panels. All data were collected at room temperature with a constant magnetic flux density  $\mu_0 H = 1 \text{ T}$ . A linear slope was subtracted from the data. A  $\sin^2(\alpha, \beta)$  modulation of  $\rho$  is evident only for the ip and oopj rotations, indicating the presence of a magnetoresistance, having a symmetry consistent with spin Hall magnetoresistance.

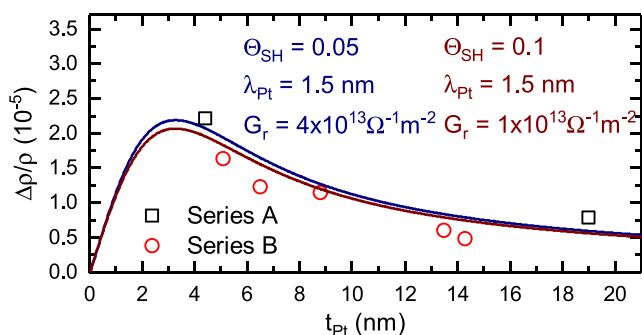


FIG. 3. The magnitude of the SMR as a function of the Pt thickness is depicted here for the two sample sets. The established thickness dependence of the SMR is shown for two parameter sets as dark blue and dark red lines. The parameters adapted from Althammer *et al.*<sup>7</sup> are summarized above the data.

In the ALD grown samples, the interface quality is most likely affected by the organic constituents of the precursor,<sup>16</sup> making novel approaches in the pre-treatment of the YIG films prior to deposition necessary.

We would like to point out that a dependence of  $\Theta_{\text{SH}} \propto \rho$  and  $\lambda \propto \rho^{-1}$  on the resistivity  $\rho$  has been reported in the literature.<sup>23–25</sup> Since the SMR depends on the product of  $\Theta_{\text{SH}}$  and  $\lambda$  [c.f. Eq. (2)], we here chose to take these parameters as constants for simplicity. The dependence of the spin transport parameters on  $\rho$  cannot be extracted from the SMR in the lowest order.

In summary, we presented magnetoresistive measurements on YIG/Pt heterostructures, where the Pt is deposited via ALD. Our data suggest the presence of SMR and good electrical properties of the Pt films which are comparable with those of sputtered films. Therefore, we demonstrate the possibility of depositing high-quality Pt with ALD. This implies the technological feasibility of 3D conformal coating with spin-Hall-active materials, opening the door to spin transport experiments in non-planar surface geometries. However, because organic constituents are used in ALD precursors, further efforts to improve the YIG/Pt interface are necessary in order to obtain mixing conductance values that are comparable to those of platinum films deposited in ultra- high vacuum.

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